

Chapter 2: Time Value of Money

2.1) $I = iPN = (0.09)(\$3,000)(5) = \$1,350$

2.2)

- Simple interest:

$$F = P(1 + iN)$$

$$\$4,000 = \$2,000(1 + 0.08N)$$

$$N = 12.5 \text{ years (or 13 years)}$$

- Compound interest:

$$\$4,000 = \$2,000(1 + 0.07)^N$$

$$2 = 1.07^N$$

$$\log 2 = N \log 1.07$$

$$N = 10.24 \text{ years (or 11 years)}$$

2.3)

- Simple interest:

$$I = iPN = (0.07)(\$10,000)(20)$$

$$= \$14,000$$

- Compound interest:

$$I = P[(1 + i)^N - 1] = \$10,000[(1.07)^{20} - 1]$$

$$= \$28,696.84$$

2.4)

- Compound interest:

$$F = \$1,000(1 + 0.06)^5$$

$$= \$1,338.23$$

- Simple interest:

$$F = \$1,000(1 + 0.07(5))$$

$$= \$1,350$$

The simple interest option is better.

2.5)

- Loan balance calculation:

End of period	Principal Payment	Interest Payment	Remaining Balance
0	\$0.00	\$0.00	\$5,000.00
1	\$835.46	\$450.00	\$4,164.54
2	\$910.65	\$374.81	\$3,253.89
3	\$992.61	\$292.85	\$2,261.28
4	\$1,081.94	\$203.52	\$1,179.33
5	\$1,179.32	\$106.14	\$0.00

$$2.6) \quad P = \$8,000(P / F, 8\%, 5) = \$8,000(0.6806) = \$5,444.8$$

$$2.7) \quad F = \$20,000(F / P, 10\%, 2) = \$20,000(1.21) = \$24,200$$

2.8)

- Alternative 1

$$P = \$100$$

- Alternative 2

$$P = \$120(P / F, 8\%, 2) = \$120(0.8573) = \$102.88$$

- Alternative 2 is preferred

$$2.9) \quad (a) \quad F = \$7,000(F / P, 9\%, 8) = \$7,000(1.9926) = \$13,948.2$$

$$(b) \quad F = \$1,250(F / P, 4\%, 12) = \$1,250(1.6010) = \$2,001.25$$

$$(c) \quad F = \$5,000(F / P, 7\%, 31) = \$5,000(8.1451) = \$40,725.5$$

$$(d) \quad F = \$20,000(F / P, 6\%, 7) = \$20,000(1.5036) = \$30,072$$

$$2.10) \quad (a) \quad P = \$4,500(P / F, 7\%, 6) = \$4,500(0.6663) = \$2,998.35$$

$$(b) \quad P = \$6,000(P / F, 8\%, 15) = \$6,000(0.3152) = \$1,891.2$$

$$(c) \quad P = \$20,000(P / F, 9\%, 5) = \$20,000(0.6499) = \$12,998$$

$$(d) \quad P = \$12,000(P / F, 10\%, 8) = \$12,000(0.4665) = \$5,598$$

2.11) (a) $P = \$6,000(P / F, 8\%, 5) = \$6,000(0.6806) = \$4,083.6$

(b) $F = \$15,000(F / P, 8\%, 4) = \$15,000(1.3605) = \$20,407.5$

2.12)

$$F = 3P = P(1 + 0.07)^N$$

$$\log 3 = N \log 1.07$$

$$N = 16.24 \text{ years (or 17 years)}$$

2.13)

$$F = 2P = P(1 + 0.12)^N$$

- $\log 2 = N \log 1.12$

$$N = 6.12 \text{ years}$$

- Rule of 72:

$$72 / 12 = 6 \text{ years}$$

2.14)

$$P = \$35,000(P / F, 9\%, 4) + \$10,000(P / F, 9\%, 2)$$

$$= \$35,000(0.7084) + \$10,000(0.8417)$$

$$= \$33,211$$

2.15)

- Simple interest:

$$I = iPN = (0.1)(\$1,000)(3) = \$300$$

- Compound interest:

$$I = P[(1 + i)^N - 1] = \$1,000[(1 + .095)^3 - 1]$$

$$= \$312.93$$

- Susan's balance will be greater by \$12.93.

2.16) $P = \frac{\$3,000}{1.06^2} + \frac{\$3,500}{1.06^3} + \frac{\$4,000}{1.06^4} + \frac{\$6,000}{1.06^5} = \$13,260.58$

2.17)

$$F = \$1,000(F / P, 8\%, 10) + \$1,500(F / P, 8\%, 8)$$

$$+ \$2,000(F / P, 8\%, 6)$$

$$= \$8,109.05$$

2.18)

$$\begin{aligned}
 P &= \$3,000,000 + \$2,400,000(P/A, 8\%, 5) \\
 &\quad + \$3,000,000(P/A, 8\%, 5)(P/F, 8\%, 5) \\
 &= \$20,734,774.86
 \end{aligned}$$

2.19)

$$\begin{aligned}
 P &= \$3,000(P/F, 9\%, 2) + \$4,000(P/F, 9\%, 5) \\
 &\quad + \$5,000(P/F, 9\%, 7) \\
 &= \$7,859.7
 \end{aligned}$$

2.20)

- Method 1:

$$\begin{aligned}
 F &= \$2,000(1.05)(1.1)(1.15) + \$3,000(1.1)(1.15) + \$5,000 \\
 &= \$11,451.5
 \end{aligned}$$

- Method 2:

$$\begin{aligned}
 F &= \overbrace{(\$2,000(1.05) + \$3,000)}^{\$6,451.50} (1.10)(1.15) + \$5,000 \\
 &\quad \underbrace{\hspace{1.5cm}}_{\$5,100} \\
 &= \$11,451.50
 \end{aligned}$$

2.21)

$$\begin{aligned}
 \$150,000 &= \$20,000(P/A, 9\%, 5) - \$10,000(P/F, 9\%, 3) + X(P/F, 9\%, 6) \\
 X &= \$134,046.98
 \end{aligned}$$

2.22)

$$\begin{aligned}
 F = \$80,000 &= \$10,000(1.08)^5 + \$12,000(1.08)^3 + X(1.08)^2 \\
 X &= \$43,029.99
 \end{aligned}$$

2.23)

$$\begin{aligned}
 100(1.08)^4 &= 8(1.08)^3 + 9(1.08)^2 + 10(1.08) + 11 + X \\
 X &= \$93.67
 \end{aligned}$$

This is the minimum selling price. So if John can sell the stock for a higher price than \$93.67, his return on investment will be higher than 8%.

$$\begin{aligned}
 2.24) \quad (a) \quad F &= \$3,000(F/A, 7\%, 8) = \$3,000(10.2598) = \$30,779.4 \\
 (b) \quad F &= \$3,000(F/A, 7\%, 8)(1.07) = \$32,933.96
 \end{aligned}$$

- 2.25) (a) $F = \$5,000(F / A, 6\%, 6) = \$5,000(6.9753) = \$34,876.5$
 (b) $F = \$9,000(F / A, 7.25\%, 9) = \$108,928.76$
 (c) $F = \$12,000(F / A, 8\%, 25) = \$12,000(73.1059) = \$877,270.8$
 (d) $F = \$6,000(F / A, 9.75\%, 10) = \$94,485.71$

- 2.26) (a) $A = \$15,000(A / F, 5\%, 13) = \$15,000(0.0565) = \$847.5$
 (b) $A = \$20,000(A / F, 6\%, 8) = \$20,000(0.1010) = \$2,020$
 (c) $A = \$5,000(A / F, 8\%, 25) = \$5,000(0.0137) = \$68.5$
 (d) $A = \$4,000(A / F, 6.85\%, 8) = \391.98

2.27)

$$\begin{aligned} \$35,000 &= \$3,000(F / A, 6\%, N) \\ (F / A, 6\%, N) &= 11.6666 \\ \frac{(1+0.06)^N - 1}{0.06} &= 11.6666 \\ N \cdot \log(1.06) &= \log(1.7) \end{aligned}$$

$$N = 9.11 \text{ years}$$

2.28)

$$\begin{aligned} \$10,000 &= A(F / A, 7\%, 5) \\ A &= \$1,738.92 \end{aligned}$$

2.29)

$$\begin{aligned} F &= \$500(1.1)^{10} + \$1,000(1.1)^8 + \$1,000(1.1)^6 \\ &\quad + \$1,000(1.1)^4 + \$1,000(1.1)^2 + \$1,000 \\ &= \$8,886.12 \end{aligned}$$

- 2.30) (a) $A = \$15,000(A / P, 8\%, 5) = \$15,000(0.2505) = \$3,757.5$
 (b) $A = \$3,500(A / P, 9.5\%, 4) = \$1,092.22$
 (c) $A = \$8,000(A / P, 11\%, 3) = \$8,000(0.4092) = \$3,273.6$
 (d) $A = \$25,000(A / P, 6\%, 20) = \$25,000(0.0872) = \$2,180$

2.31)

- Equal annual payment amount:

$$A = \$20,000(A / P, 10\%, 3) = \$20,000(0.4021) = \$8,042$$

- Loan balance calculation:

End of period	Principal Payment	Interest Payment	Remaining Balance
0	\$0.00	\$0.00	\$20,000.00
1	\$6,042.00	\$2,000.00	\$13,958.00
2	\$6,646.20	\$1,395.80	\$7,311.80
3	\$7,310.82	\$731.18	\$0

Interest payment for the second year = \$1,395.80

- 2.32) (a) $P = \$5,000(P / A, 6\%, 8) = \$5,000(6.2098) = \$31,049$
 (b) $P = \$7,500(P / A, 9\%, 10) = \$7,500(6.4177) = \$48,132.75$
 (c) $P = \$1,500(P / A, 7.25\%, 6) = \$7,094.96$
 (d) $P = \$9,000(P / A, 8.75\%, 30) = \$94,551.83$

2.33) (a) $(A / P, 6.25\%, 36) = \frac{0.0625(1 + 0.0625)^{36}}{(1 + 0.0625)^{36} - 1} = 0.07044$
 (b) $(P / A, 9.25\%, 125) = \frac{(1 + 0.0925)^{125} - 1}{0.0925(1 + 0.0925)^{125}} = 10.81064$

2.34) $F = \$400(F / A, 9\%, 15)(1.09) = \$400(29.3609)(1.09) = \$12,801.35$

2.35)

$$\begin{aligned}
 F &= F_1 + F_2 \\
 &= \$5,000(F / A, 8\%, 5) + \$2,000(F / G, 8\%, 5) \\
 &= \$5,000(F / A, 8\%, 5) + \$2,000(A / G, 8\%, 5)(F / A, 8\%, 5) \\
 &= \$5,000(5.8666) + \$2,000(1.8465)(5.8666) \\
 &= \$50,998.35
 \end{aligned}$$

2.36)

$$\begin{aligned}
 F &= \$1,200(F / A, 9\%, 5) - \$200(F / G, 9\%, 5) \\
 &= \$1,200(F / A, 9\%, 5) - \$200(P / G, 9\%, 5)(F / P, 9\%, 5) \\
 &= \$1,200(5.9847) - \$200(7.1110)(1.5386) \\
 &= \$4,993.44
 \end{aligned}$$

2.37)

$$\begin{aligned}
 P &= \$100(P/F, 8\%, 1) + \$150(P/F, 8\%, 3) \\
 &\quad + \$200(P/F, 8\%, 5) + \$250(P/F, 8\%, 7) \\
 &\quad + \$300(P/F, 8\%, 9) + \$350(P/F, 8\%, 11) \\
 &= \$793.83
 \end{aligned}$$

2.38)

$$\begin{aligned}
 A &= \$15,000 - \$3,000(A/G, 9\%, 10) \\
 &= \$15,000 - \$3,000(3.7978) \\
 &= \$3,606.6
 \end{aligned}$$

2.39)

$$\begin{aligned}
 P &= \$1,000(P/A, 9\%, 8) + \$250(P/G, 9\%, 8) \\
 &= \$1,000(5.5348) + \$250(16.8877) \\
 &= \$9,756.73
 \end{aligned}$$

2.40)

$$\begin{aligned}
 C(P/G, 12\%, 6) &= \$800(F/A, 12\%, 4) \\
 &\quad + [\$1,000 - \$200(P/G, 12\%, 4)](F/P, 12\%, 4) \\
 C(8.9302) &= \$800(4.7793) \\
 &\quad + [\$1,000 - \$200(4.1273)](1.5735) \\
 C &= \$458.90
 \end{aligned}$$

2.41) (a)

$$\begin{aligned}
 P &= \$3,000,000(P/A_1, -10\%, 12\%, 7) \\
 &= \$3,000,000 \cdot \frac{1 - (1 - 0.1)^7 (1 + 0.12)^{-7}}{0.12 - (-0.1)} \\
 &= \$10,686,037.81
 \end{aligned}$$

(b) Note that the oil price increases at the annual rate of 5% while the oil production decreases at the annual rate of 10%. Therefore, the annual revenue can be expressed as follows:

$$\begin{aligned}
 A_n &= \$30(1 + 0.05)^{n-1} 100,000(1 - 0.10)^{n-1} \\
 &= \$3,000,000(0.945)^{n-1} \\
 &= \$3,000,000(1 - 0.055)^{n-1}
 \end{aligned}$$

This revenue series is equivalent to a decreasing geometric gradient series with $g = -5.5\%$.

Instructor Solutions Manual to accompany Fundamentals of Engineering Economics, Second Edition, by Chan S. Park.

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N	A_n
1	\$3,000,000
2	\$2,835,000
3	\$2,679,075
4	\$2,531,726
5	\$2,392,481
6	\$2,260,894
7	\$2,136,545

$$\begin{aligned}
 P &= \$3,000,000(P/A_1, -5.5\%, 12\%, 7) \\
 &= \$3,000,000 \cdot \frac{1 - (1 - 0.055)^7 (1 + 0.12)^{-7}}{0.12 - (-0.055)} \\
 &= \$11,923,948.35
 \end{aligned}$$

(c) Computing the present worth of the remaining series (A_4, A_5, A_6, A_7) at the end of period 3 gives

$$\begin{aligned}
 P &= \$2,531,730(P/A_1, -5.5\%, 12\%, 4) \\
 &= \$2,531,730 \cdot \frac{1 - (1 - 0.055)^4 (1 + 0.12)^{-4}}{0.12 - (-0.055)} \\
 &= \$7,134,825.54
 \end{aligned}$$

2.42)

$$\begin{aligned}
 P &= \sum_{n=1}^{20} A_n (1+i)^{-n} \\
 &= \sum_{n=1}^{20} (2,000,000)n(1.06)^{n-1}(1.06)^{-n} \\
 &= (2,000,000 / 1.06) \sum_{n=1}^{20} n \left(\frac{1.06}{1.06}\right)^n \\
 &= (2,000,000 / 1.06) \sum_{n=1}^{20} n \\
 &= (2,000,000 / 1.06) \frac{20(21)}{2} \\
 &= \$396,226,415.1
 \end{aligned}$$

2.43) (a) The withdrawal series would be:

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Period	Withdrawal
11	\$3,000
12	\$3,000(1.06)
13	\$3,000(1.06) ²
14	\$3,000(1.06) ³
15	\$3,000(1.06) ⁴

Equivalent worth of the withdrawal series at period 10, using $i = 8\%$:

$$\begin{aligned}
 P &= \$3,000(P / A, 6\%, 8\%, 5) \\
 &= \$3,000 \cdot \frac{1 - (1 + 0.06)^5 (1 + 0.08)^{-5}}{0.08 - (0.06)} \\
 &= \$13,383.92
 \end{aligned}$$

Assuming that each deposit is made at the end of each year, the following equivalence must be hold:

$$\begin{aligned}
 \$13,384 &= A(F / A, 8\%, 10) \\
 &= 14.4866A \\
 A &= \$923.88
 \end{aligned}$$

(b) Equivalent present worth of the withdrawal series at 6%

$$\begin{aligned}
 P &= \$3,000(P / A, 6\%, 6\%, 5) = \$3,000 \frac{5}{1 + 0.06} = \$14,150.94 \\
 \$14,151 &= A(F / A, 6\%, 10) \\
 &= 13.1808A \\
 A &= \$1,073.60
 \end{aligned}$$

2.44)

$$\begin{aligned}
 P &= [\$100(F / A, 10\%, 8) + \$50(F / A, 10\%, 6) \\
 &\quad + \$50(F / A, 10\%, 4)](P / F, 10\%, 8) \\
 &= [\$100(11.4359) + \$50(7.7156) \\
 &\quad + \$50(4.6410)](0.4665) \\
 &= \$821.70
 \end{aligned}$$

2.45) Select (a).

2.46)

$$\begin{aligned}
 P(1.1) + \$500 &= \$300(P / F, 10\%, 2) \\
 &\quad + \$300(P / F, 10\%, 3) + \$800(P / F, 10\%, 4) \\
 &= \$300(0.8264) \\
 &\quad + \$300(0.7513) + \$800(0.6830) \\
 P &= \$472.46
 \end{aligned}$$

2.47)

Computing the equivalent worth at period 3 will require only two different types of interest factors.

$$\begin{aligned}
 V_{1,3} &= \$120(P / A, 10\%, 5)(F / P, 10\%, 3) \\
 &= \$120(3.7908)(1.3310) \\
 &= \$605.466 \\
 V_{2,3} &= A(P / A, 10\%, 2)(F / P, 10\%, 3) + A(P / A, 10\%, 2) \\
 &= A(1.7355)(1.3310) + A(1.7355) \\
 &= 4.04545A \\
 A &= \$605.466 / 4.04545 \\
 &= \$149.67
 \end{aligned}$$

2.48)

$$\begin{aligned}
 P_{1,1} &= \$200(P / A, 10\%, 4) - 100(P / A, 10\%, 2) \\
 &= \$200(3.1699) - 100(1.7355) \\
 &= 460.43
 \end{aligned}$$

$$\begin{aligned}
 P_{2,1} &= X + X(P / A, 10\%, 4) \\
 &= X + X(3.1699) \\
 &= 4.1699X
 \end{aligned}$$

$$\begin{aligned}
 P_{1,1} &= P_{2,1} \\
 \$460.43 &= 4.1699X \\
 X &= \$110.42
 \end{aligned}$$

2.49)

$$\begin{aligned}
 P_1 &= \$50(P / A, 10\%, 4) + \$35(P / A, 10\%, 2)(P / F, 10\%, 2) \\
 &= \$50(3.1699) + \$35(1.7355)(0.8264) \\
 &= 208.6926
 \end{aligned}$$

$$\begin{aligned}
 P_2 &= C(P / A, 10\%, 4) + C(P / A, 10\%, 2)(P / F, 10\%, 1) \\
 &= C(3.1699) + C(1.7355)(0.9091) \\
 &= 4.7476C
 \end{aligned}$$

$$P_1 = P_2$$

$$C = \$43.96$$

2.50)

$$C(F / A, 9\%, 8) = \$5,000(P / A, 9\%, 2)$$

$$C(11.0285) = \$5,000(1.7591)$$

$$C = \$797.52$$

2.51) The original cash flow series is

n	A_n
0	\$0
1	\$800
2	\$820
3	\$840
4	\$860
5	\$880
6	\$900
7	\$920
8	\$300
9	\$300
10	\$300 - \$500

2.52)

$$\begin{aligned}
 2C + C(P / A, 12\%, 7)(P / F, 12\%, 1) \\
 = \$1,200(P / A, 12\%, 8) - 400(P / A, 12\%, 4)
 \end{aligned}$$

$$\begin{aligned}
 2C + C(4.5638)(0.8929) \\
 = \$1,200(4.9676) - 400(3.0373)
 \end{aligned}$$

$$6.075C = \$4,746.20$$

$$C = \$781.27$$

2.53)

$$200(1.06)(1.08)(1.12)(1.15)$$

$$+ X(1.08)(1.12)(1.15)$$

$$+ \$300(1.15)$$

$$= \$1000$$

$$247.9 + 1.39104X + 345 = 1000$$

$$1.39104X = 360.1$$

$$X = \$258.87$$

2.54) Computing the equivalent worth at $n = 5$,

$$X = \$5,000(F / A, 10\%, 5) + \$5,000(P / A, 10\%, 5)$$

$$= \$5,000(6.1051) + \$5,000(3.7908)$$

$$= \$49,475.5$$

2.55)

$$A(F / A, 8\%, 18) = \$20,000 + \$20,000(P / A, 8\%, 3)$$

$$A(37.4502) = \$20,000 + \$20,000(2.5771)$$

$$= \$71542$$

$$A = \$1910.32$$

2.56)

$$P_{1,0} = \$500 + \$500(P / A, 10\%, 5)$$

$$= \$500 + \$500(3.7908)$$

$$= \$2,395.4$$

$$P_{2,0} = X[(P / F, 10\%, 1) + (P / F, 10\%, 4)]$$

$$= X[(0.9091) + (0.6830)]$$

$$= 1.5921X$$

$$X = \$1,504.55$$

2.57)

$$\begin{aligned}
 P_{1,2} &= X(P / F, 8\%, 3) \\
 &= X(0.7938)
 \end{aligned}$$

$$\begin{aligned}
 P_{2,2} &= 800(P / A, 8\%, 10) \\
 &= 800(6.7101) \\
 &= 5368.08
 \end{aligned}$$

$$X = 6,762.51$$

2.58)

$$\begin{aligned}
 C(P / A, 9\%, 5)(P / F, 9\%, 1) &= \$4,000 \\
 C(3.8897)(0.9174) &= \$4,000 \\
 C &= \$1,120.95
 \end{aligned}$$

2.59)

$$\begin{aligned}
 &P(1.05)(1.08)(1.1)(1.06) \\
 &= \$1,000(1.08)(1.1)(1.06) + \$1,500(1.1)(1.06) \\
 &\quad + \$1,000(1.06) + \$1000 \\
 P(1.322244) &= \$5,068.28 \\
 P &= \$3,833.09
 \end{aligned}$$

2.60)

- Exact:

$$\begin{aligned}
 2P &= P(1+i)^5 \\
 2 &= (1+i)^5 \\
 \log 2 &= 5 \log(1+i) \\
 i &= 14.87\%
 \end{aligned}$$
- Rule of 72:

$$\begin{aligned}
 72 / i &= 5 \text{ years} \\
 i &= 14.4\%
 \end{aligned}$$

2.61)

$$\begin{aligned}
 P_1 &= \$150(P / A, i, 5) - \$50(P / F, i, 1) \\
 &= \$150 \left(\frac{(1+i)^5 - 1}{i(1+i)^5} \right) - \$50 \cdot (1+i)^{-1}
 \end{aligned}$$

- $P_2 = \frac{\$200}{(1+i)} + \frac{\$150}{(1+i)^2} + \frac{\$50}{(1+i)^3} + \frac{\$200}{(1+i)^4} + \frac{\$50}{(1+i)^5}$
- $P_1 = P_2$ and solving i with Excel Goal Seek function,
 $i = 14.96\%$

2.62)

$$\begin{aligned}\$35,000 &= \$10,000(F / P, i, 5) \\ &= \$10,000(1+i)^5 \\ i &= 28.47\%\end{aligned}$$

2.63) The equivalent future worth of the prize payment series at the end of Year 20 (or beginning of Year 21) is

$$\begin{aligned}F_1 &= \$1,952,381(F / A, 6\%, 20) \\ &= \$1,952,381(36.7856) \\ &= \$71,819,506.51\end{aligned}$$

The equivalent future worth of the lottery receipts is

$$\begin{aligned}F_2 &= (\$36,100,000 - \$1,952,381)(F / P, 6\%, 20) \\ &= (\$36,100,000 - \$1,952,381)(3.2071) \\ &= \$109,514,828.9\end{aligned}$$

The resulting surplus at the end of Year 20 is

$$\begin{aligned}F_2 - F_1 &= \$109,514,828.9 - \$71,819,506.51 \\ &= \$37,695,322.4\end{aligned}$$

2.64)

$$\begin{aligned}&\$1,000(F / P, 9.4\%, 5) + \$500(F / A, 9.4\%, 5) \\ &= \$1,000((1 + 0.094)^5) + \$500\left(\frac{(1 + 0.094)^5 - 1}{0.094}\right) \\ &= \$1,000(1.5671) + \$500(6.0326) \\ &= \$4,583.4\end{aligned}$$

$$\begin{aligned}&\$4,583.4(F / P, 9.4\%, 60) \\ &= \$4,583.4((1 + 0.094)^{60}) \\ &= \$4,583.4(219.3) \\ &= \$1,005,141.21\end{aligned}$$

The main question is whether or not the U.S. government will be able to invest the social security deposits at 9.4% interest over 60 years.

2.65)

$$\begin{aligned}
 P_{\text{Contract}} &= \$3,875,000 + \$3,125,000(P/F, 6\%, 1) \\
 &\quad + \$5,525,000(P/F, 6\%, 2) + \cdots \\
 &\quad + \$8,875,000(P/F, 6\%, 7) \\
 &= \$3,875,000 + \$2,550,000(0.9434) \\
 &\quad + \$5,525,000(0.8900) + \cdots \\
 &\quad + \$8,875,000(0.6651) \\
 &= \$39,548,212.5
 \end{aligned}$$